# Crystal Chemistry in the System $\mathrm{MSbO}_{3}{ }^{*}$ 

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#### Abstract

Cubic, disordered phases of the compounds $\mathrm{MSbO}_{3}(\mathrm{M}=\mathrm{Li}, \mathrm{Na}, \mathrm{K}, \mathrm{Rb}, \mathrm{Tl}$, and Ag$)$ have been investigated. $\mathrm{KSbO}_{3}$ is readily synthesized in the disordered, cubic structure at high pressure, and the other isomorphic compounds were obtained by ion exchange. The structures of $\mathrm{NaSbO}_{3}$ and $\mathrm{AgSbO}_{3}$, which have space group $\operatorname{Im} 3$, were solved by X-ray single-crystal analysis. The structures contain an essentially rigid $\mathrm{SbO}_{3}$ subarray consisting of pairs of edge-shared octahedra sharing common corners. Within this subarray, face-shared octahedra form $\langle 111\rangle$ tunnels that intersect at the origin and body center of the unit cell, and the $\mathrm{M}^{+}$ions are randomly distributed over two positions within these tunnels. Ordered, cubic phases have the primitive-cubic space group Pn 3 . The two M positions are different for $\mathrm{Na}^{+}$and for $\mathrm{Ag}^{+}$ions. At one of the $\mathrm{Ag}^{+}$wion positions, the $\mathrm{Ag}-\mathrm{O}$ bond length is only $2.26 \AA$, consistent with the gray-black color of $\mathrm{AgSbO}_{3}$. Deformation of the $4 d^{10} \mathrm{Ag}^{+}$-ion core by $4 d-5$ s hybridization appears to be induced by $\mathrm{Ag}-\mathrm{O}$ covalent bonding. This conclusion is compatible with the observation that ion exchange is reversible for all compounds but $\mathrm{AgSbO}_{3}$. Several properties of these compounds are compared with the super ionic conductors $\mathrm{M}_{2} \mathrm{O} \cdot 11 \mathrm{Al}_{2} \mathrm{O}_{3} \beta$-alumina.


## I. Introduction

Unlike the $\mathrm{M}^{+} \mathrm{NbO}_{3}$ and $\mathrm{M}^{+} \mathrm{TaO}_{3}$ compounds, the $\mathrm{M}^{+} \mathrm{SbO}_{3}$ compounds do not form structures having $180^{\circ} \mathrm{Sb}-\mathrm{O}-\mathrm{Sb}$ linkages, presumably because this is inhibited by covalency (1). Thus $\mathrm{KSbO}_{3}$ does not form the cubic perovskite structure. At atmospheric pressure it generally has the rhombohedral ilmenite structure. However, Spiegelberg (2) reported synthesizing two cubic phases of $\mathrm{KSbO}_{3}$ by annealing for 3 wk at $1000^{\circ} \mathrm{C}$. One of these was primitive, with space group Pn3. The other was body-centered, but Spiegelberg was unable to determine its space group.
In the primitive-cubic $\mathrm{KSbO}_{3}$, pairs of $\mathrm{SbO}_{6}$ octahedra share common edges to form $\mathrm{Sb}_{2} \mathrm{O}_{10}$ clusters (2). These clusters share corners to form the network shown in Fig. 1. The network contains empty tunnels of face-shared octahedra that run parallel to the $\langle 111\rangle$ directions and intersect at the center of the front face in Fig. 1. This origin is itself a large octahedral interstice, and along any $\langle 111\rangle$ direction there are three additional

[^0]octahedral positions between the origin and its body-center equivalent. Each of the shared faces along the tunnels consists of either $\mathrm{O}_{1}$ or $\mathrm{O}_{2}$


Fig. 1. The cubic $\mathrm{SbO}_{3}$ matrix found by Spiegelberg (2) for cubic $\mathrm{KSbO}_{3}$ having the space group Pn 3 and ordered $\mathbf{K}^{+}$-ion positions.
oxygen atoms. The order of the faces is $\mathrm{O}_{1}-\mathrm{O}_{2}-$ $\mathrm{O}_{2}-\mathrm{O}_{1}$, and the triangular area of an $\mathrm{O}_{1}$ face is somewhat larger than that of an $\mathrm{O}_{2}$ face. The primitive unit cell contains $\mathrm{K}_{12} \mathrm{Sb}_{12} \mathrm{O}_{36}$, and the $\mathrm{K}^{+}$ions are ordered within the octahedral sites of these tunnels: eight in $\mathrm{O}_{1}-\mathrm{O}_{2}$ octahedra along four tetrahedral directions from the origin, and four in $\mathrm{O}_{2} \mathrm{O}_{2}$ octahedra along the remaining four directions.

The body-centered cell is closely related to the primitive unit cell. A body-centered-cubic $I 23$ phase containing a network similar to the one in Fig. 1 has been reported (3) for $\mathrm{La}_{4} \mathrm{ORe}_{6} \mathrm{O}_{18}$. In this structure an oxygen is located at the origin and four $\mathrm{La}^{3+}$ ions occupy $\mathrm{O}_{1}-\mathrm{O}_{2}$ octahedra in $[1,1,1],[\overline{1}, \overline{1}, 1],[\overline{1}, 1, \overline{1}],[1, \overline{1}, \overline{1}]$ directions. It is therefore reasonable to assume that the bodycentered form of $\mathrm{KSbO}_{3}$ contains the $\mathrm{SbO}_{3}$ network of Fig. 1 with the $\mathbf{K}^{+}$ions disordered over the octahedral sites of the tunnels. This assignment gives space group Im3.

The possibility of alkali-ion exchange was suggested by the cubic $\mathrm{KSbO}_{3}$ structures. The tunnels of face-shared octahedra running parallel to the $\langle 111\rangle$ directions are not completely occupied, so high alkali-ion conductivity may be anticipated, provided the $\mathrm{M}^{+}$ion is small enough to move through the $\mathrm{O}_{2}$ faces. Since the $\mathrm{O}_{2}-\mathrm{O}_{2}$ and $\mathrm{O}_{1}-\mathrm{O}_{1}$ octahedra are flattened, making relatively open $\mathrm{O}_{1}$ and $\mathrm{O}_{2}$ faces, the structure also suggests that the alkali-ion conductivity may be comparable to that of sodium $\beta$-alumina, $\mathrm{Na}_{2} \mathrm{O} \cdot 11 \mathrm{Al}_{2} \mathrm{O}_{3}$. Therefore, in addition to the structure refinements for several $\mathrm{MSbO}_{3}$ compounds, we compare their properties with those of $\beta$-alumina.

## II. Preparation

The cubic forms of $\mathrm{KSbO}_{3}$ were prepared from the ilmenite form in a high-pressure "belt" apparatus (4) capable of developing 90 kbar and equipped with an internal graphite heater. The ilmenite phase was subjected to pressures in excess of 20 kbar and then to a temperature of $700^{\circ} \mathrm{C}$ for 30 min . The specimen was subsequently quenched to room temperature before the pressure was released. This treatment normally yielded the disordered, body-centered form $\operatorname{Im} 3$ of cubic $\mathrm{KSbO}_{3}$. Subsequent heat treatment $\left(1200^{\circ} \mathrm{C}\right.$ for 16 hr ) of this form at atmospheric pressure yielded the ordered Pn 3 form.
$\mathrm{RbSbO}_{3}$ and $\mathrm{TlSbO}_{3}$ were prepared from the products of stoichiometric amounts of $\mathrm{Rb}_{2} \mathrm{CO}_{3}$
or $\mathrm{Tl}_{2} \mathrm{CO}_{3}$ and $\mathrm{Sb}_{2} \mathrm{O}_{3}$ air-fired at $900^{\circ} \mathrm{C}$. The products were encapsulated in gold foil and subjected to the desired pressure in the belt apparatus. The temperature was raised to $900^{\circ} \mathrm{C}$ for 30 min and quenched before the pressure was released. At $20 \mathrm{kbar}, \mathrm{RbSbO}_{3}$ was obtained in the ordered Pn3 form. Considerably higher pressure gave the disordered $\operatorname{Im} 3$ form. Pressures in excess of 20 kbar yielded a cubic $\mathrm{TlSbO}_{3}$ phase having a doubled cell edge. Oscillation and Weissenberg pictures of a single crystal showed a face-centered-cubic cell with diffraction symmetry $m 3$, which indicates space group $F 23$ or Fm3.

Attempts to prepare $\mathrm{NaSbO}_{3}, \mathrm{AgSbO}_{3}$ and $\mathrm{LiSbO}_{3}$ by the same high-pressure technique gave, respectively, an ilmenite, a pyrochlore, and an orthorhombic phase. However, we have been able to prepare each of these compounds in the body-centered $\operatorname{Im} 3$ phase by an ion-exchange method. A cubic $\mathrm{KSbO}_{3}$ phase was mixed with molten $\mathrm{MNO}_{3}(\mathrm{M}=\mathrm{Li}, \mathrm{Na}, \mathrm{Rb}, \mathrm{Tl}$, or Ag$)$ in about $1: 10$ molar ratios for a few hours. In each case, the $\mathrm{K}^{+}$ions appeared to be completely replaced by the $\mathrm{M}^{+}$ions, since the X -ray powder pattern showed significant changes in the cell parameters (see Table IV) and the final cell parameter was independent of the initial compound: $\mathrm{KSbO}_{3}$ or $\mathrm{TlSbO}_{3}$, for example. Except for $\mathrm{AgSbO}_{3}$, the process is reversible. If one of the other $\mathrm{MSbO}_{3}$ phases is mixed with molten $\mathrm{KNO}_{3}$, for example, the $\operatorname{Im} 3 \mathrm{KSbO}_{3}$ phase is recovered and has the initial cell size.

Structure determinations of $\mathrm{NaSbO}_{3}$ and $\mathrm{AgSbO}_{3}$ were made on single crystals prepared from single crystals of $\mathrm{TlSbO}_{3}$ by ion exchange in molten $\mathrm{NaNO}_{3}$ and $\mathrm{AgNO}_{3}$, respectively. The single crystals of $\mathrm{TlSbO}_{3}$ were selected from the powder product of a high-pressure reaction ( 20 kbar at $700^{\circ} \mathrm{C}$ for 30 min ) of the product of an $800^{\circ} \mathrm{C}$ reaction of $\mathrm{Tl}_{2} \mathrm{CO}_{3}$ and $\mathrm{Sb}_{2} \mathrm{O}_{3}$.

## III. Structure

Weissenberg photographs of single crystals of $\mathrm{NaSbO}_{3}$ and $\mathrm{AgSbO}_{3}$, prepared from $\mathrm{TlSbO}_{3}$ by ion exchange, showed they were cubic, but with the low symmetry $m 3$. Systematic absences were observed for $h+k+l=2 n+1$, consistent with space groups $I 23, I 2_{1} 3$ and $\operatorname{Im} 3$.

X-Ray intensity measurements of threedimensional data were taken to $2 \theta=60^{\circ}$ with a GE XRD-5 diffractometer using Zr -filtered MoK $\alpha$ radiation at a $5^{\circ}$ takeoff angle. Each peak
height was counted for 10 sec , and backgrounds were counted for 10 sec at $\pm 2^{\circ}$ in $2 \theta$ off the peak. The Lorentz, polarization and $\phi$-angle absorption corrections were applied. Both crystals were about 0.2 mm cube, and three-dimensional absorption corrections were considered not necessary.

A three-dimensional Patterson map was calculated and interpreted on the basis of space group $\operatorname{Im} 3$. As anticipated from the strong similarity between the powder patterns of primitive and body-centered $\mathrm{KSbO}_{3}$ as well as from the ease of ion exchange, the $\mathrm{SbO}_{3}$ network appears to be similar to Fig. 1, which was identified for the primitive-cubic $\mathrm{KSbO}_{3}$ structure. Therefore, the $\mathrm{Sb}^{5+}$-ion and $\mathrm{O}^{2-}$-ion positions obtained by Spiegelberg (2) for the Pn3 form of $\mathrm{KSbO}_{3}$ were used for the initial refinement based on $\operatorname{Im} 3$. The least-squares program gave a reliability factor $R=0.17$ for $\mathrm{NaSbO}_{3}$ and $R=$ 0.18 for $\mathrm{AgSbO}_{3}$. From the calculated structure factors based on this model, a Fourier map for $\mathrm{NaSbO}_{3}$ revealed two $\mathrm{Na}^{+}$-ion positions at ( $x, x, x$ ): a larger electron density near $x=\frac{1}{8}$ and a lower electron density at $x=\frac{1}{4}$. There was zero electron density at $(0,0,0)$, the center of the front face in Fig. 1. The Fourier map for $\mathrm{AgSbO}_{3}$ also gave two $\mathrm{Ag}^{+}$-ion positions at ( $x, x, x$ ) : a smaller electron density for $x$ approaching $\frac{1}{8}$ and a stronger about midway in the interval $\frac{1}{8}<x<\frac{1}{4}$. With these atomic positions and anisotropic temperature factors, a few refinement cycles reduced the reliability factors to $R=0.07$ for $\mathrm{NaSbO}_{3}$ for all 238 reflections and $R=0.08$ for $\mathrm{AgSbO}_{3}$ for all 138 reflections. Refinements based on the space groups $I 23$ and $I 2_{1} 3$ both gave
higher $R$ factors and unrealistic temperature factors. Therefore, the space group $\operatorname{Im} 3$ was confirmed. The scattering factors used for K , $\mathrm{Sb}^{5+}, \mathrm{O}$ are those published (5) with anomalous dispersion coefficients for Mo radiation (6). The final atomic positions, occupancy factors and anisotropic temperature factors are shown in Table I for $\mathrm{NaSbO}_{3}$, in Table II for $\mathrm{AgSbO}_{3}$. The bond distances for both compounds are shown in Table III.

It is instructive to locate the positions of the $\mathrm{M}^{+}$ions relative to the $\mathrm{O}_{1}$ and $\mathrm{O}_{2}$ faces along a $\langle 111\rangle$-axis tunnel. In $\mathrm{NaSbO}_{3}$, the normalized distance from an $\mathrm{O}_{1}^{2-}$ ion at $(0.356,0,0)$ to a $\mathrm{Na}^{+}$ ion at $(x, x, x)$ is

$$
\begin{align*}
D_{1} / a & =\left[(x-0.356)^{2}+x^{2}+x^{2}\right]^{1 / 2} \\
& =\left(3 x^{2}-0.712 x+0.1267\right)^{1 / 2}, \tag{1}
\end{align*}
$$

which gives a minimum separation ( $a=9.3775 \AA$, Table IV)

$$
\begin{equation*}
D_{1, \min }=2.726 \AA \text { at } x=0.1187 \tag{2}
\end{equation*}
$$

the center of an $\mathrm{O}_{1}$ face. Similarly, the normalized distance from an $\mathrm{O}^{2-}$ ion at $(0,0.334,0.287)$ is

$$
\begin{align*}
D_{2} / a & =\left[x^{2}+(x-0.334)^{2}+(x-0.287)^{2}\right]^{1 / 2} \\
& =\left(3 x^{2}-1.242 x+0.1939\right)^{1 / 2} \tag{3}
\end{align*}
$$

which has a minimum value

$$
\begin{equation*}
D_{2, \min }=2.40 \AA \text { at } x=0.207, \tag{4}
\end{equation*}
$$

the center of an $\mathrm{O}_{2}$ face. Since the ionic $\mathrm{Na}-\mathrm{O}$ distance is $2.42 \AA$, it is apparent that the $\mathrm{Na}^{+}$ions should move along the tunnels with a relatively small activation energy. Moreover, from Table I, the $\mathrm{Na}_{1}$ position is located at $x=0.123$, which places it near the center of an $\mathrm{O}_{1}-\mathrm{O}_{2}$ octahedron.

TABLE I
Atomic Posicions and Thermal Parameters of $\mathrm{NaSbO}_{3}$

| Atom: <br> Position: | Sb |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Occupancy |  |
| factor: |  |$\quad 12(e) \quad$| $\mathrm{O}_{1}$ |
| :---: |

TABLE II
Atomic Positions and Thermai. Parameters of $\mathrm{AgSbO}_{3}$

| Atom: <br> Position: <br> Occupancy <br> factor: | Sb <br> $12(e)$ | $\mathrm{O}_{1}$ <br> $\mathrm{i} 2(d)$ | $\mathrm{O}_{2}$ <br> $24(g)$ | $\mathrm{Ag}_{1}$ <br> $16(f)$ | $\mathrm{Ag}_{2}$ <br> $16(f)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $0.33(3)$ | $0.44(2)$ |
| $x$ | $0.8393(4)$ | $0.371(4)$ | 0 | $0.111(1)$ | $0.184(1)$ |
| $y$ | 0 | 0 | $0.296(7)$ | $0.111(1)$ | $0.184(1)$ |
| $z$ | $\frac{1}{2}$ | 0 | $0.291(4)$ | $0.111(1)$ | $0.184(1)$ |
| $\beta_{11}$ | $0.0007(4)$ | $0.002(4)$ | $0.009(5)$ | $0.013(2)$ | $0.012(1)$ |
| $\beta_{22}$ | $0.0025(5)$ | $0.006(5)$ | $0.05(1)$ | $0.013(2)$ | $0.012(1)$ |
| $\beta_{33}$ | $0.0028(5)$ | $0.002(4)$ | $0.008(5)$ | $0.013(2)$ | $0.012(1)$ |
| $\beta_{12}$ | 0 | 0 | 0 | 0 | $0.006(1)$ |
| $\beta_{13}$ | 0 | 0 | 0 | 0 | $0.006(1)$ |
| $\beta_{23}$ | 0 | 0 | $0.012(9)$ | 0 | $0.006(1)$ |

TABLE III
Bond Distances $(\AA)$ of $\mathrm{NaSbO}_{3}$ and $\mathrm{AgSbO}_{3}$

|  | $\mathrm{NaSbO}_{3}$ | $\mathrm{AgSbO}_{3}$ |
| :---: | :---: | :---: |
| Octahedron around $\mathbf{S b}^{5+}$ |  |  |
| $\mathrm{Sb}-\mathrm{O}_{1} 2 \times$ | 2.027 | 1.936 |
| $\mathrm{Sb}-\mathrm{O}_{2} 2 \times$ | 1.949 | 2.279 |
| $2 \times$ | 1.996 | 2.006 |
| Nearest $\mathrm{O}^{2-}$ neighbors |  |  |
| $\mathrm{O}_{1}-\mathrm{O}_{1} 1 \times$ | 2.692 | 2.421 |
| $\mathrm{O}_{1}-\mathrm{O}_{2} 4 \times$ | 2.864 | 3.002 |
| $\mathrm{O}_{1}-\mathrm{O}_{2} 2 \times$ | 3.202 | 2.881 |
| $\mathrm{O}_{1}-\mathrm{O}_{2} 2 \times$ | 2.701 | 2.828 |
| $\mathrm{O}_{2}-\mathrm{O}_{2} 4 \times$ | 2.774 | 2.866 |
| Neighbors of $\mathrm{Na}^{+}$ | Neighbors of $\mathbf{A g}^{+}$ |  |
| $\mathrm{Na}_{1}-\mathrm{O}_{1} 3 \times 2.730$ | $\mathrm{Ag}_{1}-\mathrm{O}_{1} 3 \times 2.858$ |  |
| $\mathrm{Na}_{1}-\mathrm{O}_{2} 3 \times 2.760$ | $\mathrm{Ag}_{1}-\mathrm{O}_{2} \mathbf{3} \times 2.644$ |  |
| $\mathrm{Na}_{2}-\mathrm{O}_{2} 6 \times 2.650$ | $\mathrm{Ag}_{2}-\mathrm{O}_{1} \mathbf{3} \times 3.014$ |  |
| $\mathrm{Na}_{1}-\mathrm{Na}_{1} 3 \times 2.303$ | $\mathrm{Ag}_{2}-\mathrm{O}_{2} 3 \times 2.260$ |  |
| $\mathrm{Na}_{1}-\mathrm{Na}_{1} 3 \times 3.257$ | $\mathrm{Ag}_{1}-\mathrm{Ag}_{2} 3 \times 2.935$ |  |
| $\mathrm{Na}_{1}-\mathrm{Na}_{2} 2 \times 2.094$ | $\mathrm{O}_{1}-\mathrm{O}_{1} 4.950$ (triangle) |  |
| $\mathrm{O}_{1}-\mathrm{O}_{1} 4.761$ (triangle) | $\mathrm{O}_{2}-\mathrm{O}_{2} 3.910$ (triangle) |  |
| $\mathrm{O}_{2}-\mathrm{O}_{2} 4.447$ (triangle) |  |  |

It is displaced from the position $x=0.127$, where $D_{1}=D_{2}$, toward the origin-presumably because of electrostatic interactions between $\mathrm{Na}^{+}$ions at neighboring $\mathrm{Na}_{1}$ positions within the tunnelsto give three $\mathrm{Na}_{1}-\mathrm{O}_{1}$ distances of $2.73 \AA$ and three $\mathrm{Na}_{1}-\mathrm{O}_{2}$ distances of $2.76 \AA$. From the
relative intensities of the electron densities at positions $\mathrm{Na}_{1}$ and $\mathrm{Na}_{2}$, it appears that a $\mathrm{Na}^{+}$ion at a $\mathrm{Na}_{2}$ position inhibits occupancy of the nearneighbor $\mathrm{O}_{1}-\mathrm{O}_{2}$ sites on opposite sides of it. Moreover, any electrostatic forces between $\mathrm{Na}^{+}$ ions produce a zero mean $\mathrm{Na}_{2}$ displacement, and

TABLE IV
Lattice Constants of $\mathrm{MSbO}_{3}$
Polymorphs with Space
Group Im3

| Compound | $a(\AA)$ |
| :--- | :---: |
| $\mathrm{AgSbO}_{3}{ }^{a}$ | $9.404(3)$ |
| $\mathrm{LiSbO}_{3}$ | $9.465(8)$ |
| $\mathrm{NaSbO}_{3}{ }^{a}$ | $9.378(3)$ |
| $\mathrm{KSbO}_{3}$ | $9.563(8)$ |
| $\mathrm{RbSbO}_{3}$ | $9.698(8)$ |
| $\mathrm{TlSbO}_{3}$ | $19.30(1)$ |

[^1]all $\mathrm{Na}_{2}-\mathrm{O}_{2}$ distances are $2.65 \AA$. Figure 2a gives a schematic representation of the random $\mathrm{Na}^{+}-$ ion distribution.

In $\mathrm{AgSbO}_{3}$, on the other hand, the $\mathrm{Ag}^{+}$ions


Fig. 2. Schematic representation of the eight〈111〉 channels branching from the origin to the neighboring body-center positions: (a) $\mathrm{NaSbO}_{3}$ and (b) $\mathrm{AgSbO}_{3}$. The $\mathrm{O}_{1}$ and $\mathrm{O}_{2}$ octahedral-site faces perpendicular to the channels are represented by straight lines. Possible distributions of $\mathbf{M}^{+}$ions over the $\mathbf{M}_{1}$ and $\mathbf{M}_{\mathbf{2}}$ positions are also indicated.
are not located at or near the centers of the $\mathrm{O}_{2}-\mathrm{O}_{2}$ or $\mathrm{O}_{1}-\mathrm{O}_{2}$ octahedra. Since

$$
\begin{align*}
& D_{1} / a=\left(3 x^{2}-0.742 x+0.1376\right)^{1 / 2}  \tag{5}\\
& D_{2} / a=\left(3 x^{2}-1.176 x+0.1729\right)^{1 / 2} \tag{6}
\end{align*}
$$

and $a=9.4038 \AA$, it follows that

$$
\begin{align*}
& D_{1, \min }=2.849 \AA \text { at } x=0.124,  \tag{7}\\
& D_{2, \min }=2.258 \AA \text { at } x=0.196 . \tag{8}
\end{align*}
$$

Therefore, the $\mathrm{Ag}_{2}$ position at $x=0.184$ is located close to an $\mathrm{O}_{2}$ face and forms an unusually short $\mathrm{Ag}-\mathrm{O}$ bond of only $2.260 \AA$. It would appear that this strong bond traps the $\mathrm{Ag}^{+}$ion, hindering its transfer to the $\mathrm{O}_{2}-\mathrm{O}_{2}$ octahedral site at $x=0.25$. At least such an explanation would account for the zero electron density at $x=0.25$ and the inability to exchange $\mathrm{Ag}^{+}$ions reversibly.

In $\mathrm{AgSbO}_{3}$, the $\mathrm{SbO}_{3}$ matrix is deformed so as to give much smaller $\mathrm{O}_{2}-\mathrm{O}_{2}$ than $\mathrm{O}_{1}-\mathrm{O}_{1}$ separations, as can be seen from Eqs. (7) and (8). In fact, $D_{1}=D_{2}$ at $x=0.081$, which is well inside the large octahedral sites of all $\mathrm{O}_{1}$ ions. The $\mathrm{Ag}_{1}$ positions at $x=0.111$ are also inside, as can be seen from Eq. (7). Since the $\mathrm{Ag}_{2}-\mathrm{O}_{2}$ distances are strikingly shorter than the $\mathrm{Ag}_{1}-\mathrm{O}_{2}$ distances, the $\mathrm{Ag}^{+}$ions should occupy preferentially the $\mathrm{Ag}_{2}$ positions. However, the $\mathrm{Ag}_{2}-\mathrm{Ag}_{2}$ separation across a common $\mathrm{O}_{2}-\mathrm{O}_{2}$ site is so short that electrostatic $\mathrm{Ag}^{+}-\mathrm{Ag}^{+}$interactions can be expected to inhibit occupancy of both positions. Therefore, the $12 \mathrm{Ag}^{+}$ions per unit cell can be distributed preferentially among only 8 of the 16 $\mathrm{Ag}_{2}$ positions. For an infinile $\mathrm{Ag}_{2}$-site preference energy, the electron-density ratio for the two sites would be $\mathrm{Ag}_{1} / \mathrm{Ag}_{2}=\frac{1}{2}$. From Table II, a ratio $\mathrm{Ag}_{1} / \mathrm{Ag}_{2}=\frac{3}{4}$ is observed, indicating a finite $\mathrm{Ag}_{2}-$ site preference energy. This leads to the random $\mathrm{Ag}^{+}$-ion distribution shown schematically in Fig. 2b. An $\mathrm{Ag}_{1}$ position at $x=0.111$ suggests that $\mathrm{Ag}^{+}-\mathrm{Ag}^{+}$pair interactions within a tunnel have been strong enough to displace one $\mathrm{Ag}^{+}$ion from an $\mathrm{Ag}_{2}$ to an $\mathrm{Ag}_{1}$ position, but that the interactions between ions at $\mathrm{Ag}_{1}$ positions have kept $x>0.081$, the position where $D_{1}=D_{2}$.

The $\mathrm{Ag}^{+}$ions at $\mathrm{Ag}_{1}$ positions appear to be ionically bound, those at $\mathrm{Ag}_{2}$ positions to be covalently bound to three $\mathrm{O}_{2}$ ions. Such a variation in $\mathrm{Ag}-\mathrm{O}$ bonding is characteristic of $\mathrm{Ag}^{+}-$ ion salts. Where the oxygens have orbitals
available for strong coordinate covalence, there a $4 d-5$ s hybridization may be induced on the $\mathrm{Ag}^{+}$ ions. Such hybridization changes the shape of the $4 d^{10}$ core from a sphere to an ellipsoid, thereby allowing stronger $\mathrm{Ag}-\mathrm{O}$ bonding along the shorter axis, or axes, of the ellipsoid by reducing the extension of the core-core repulsive forces. In black $\mathrm{Ag}_{2} \mathrm{O}$, linear $\mathrm{O}-\mathrm{Ag} \mathrm{O}$ bonding produces $\mathrm{Ag}-\mathrm{O}$ bond lengths of only $2.05 \AA$. Each $\mathrm{O}^{2-}$ ion has four near-neighbor $\mathrm{Ag}^{+}$ions in tetrahedral coordination, and $s p^{3}$ hybridization at the oxygen is coupled to $s d_{\sigma}$ hybridization at the silver to allow strongly covalent bonding. In white $\mathrm{AgClO}_{3}$, on the other hand, the oxygen atoms use all their $2 s 2 p$ orbitals to bond preferentially with the chlorine atoms, so no $4 d-5 s$ hybridization is induced on the $\mathrm{Ag}^{+}$ions and the $\mathrm{Ag}-\mathrm{O}$ separations vary from 2.47 to $2.55 \AA$. $\mathrm{Ag}-\mathrm{O}$ bond lengths of intermediate size are common. Yellow $\mathrm{Ag}_{2} \mathrm{CO}_{3}$, for example, has an $\mathrm{Ag}-\mathrm{O}$ separation of $2.30 \AA$. Interestingly, the color of the silver salts may be well correlated with the $\mathrm{Ag}-\mathrm{O}$ separation $R$. For $R>2.4 \AA$, the compounds are white, and for $R<2.25 \AA$ the compounds are black. $\mathrm{AgSbO}_{3}$, which contains an $R=2.25 \AA$, is gray-black. Compounds having $R=2.30-2.34$ are yellow or red.

Interpretation of the color changes with bond length proceeds as follows. White compounds have a large ( $\gtrsim 2.8 \mathrm{eV}$ ) energy gap $E_{g}$ between the valence and conduction bands. Black compounds have an $E_{g} \leqq 1.7 \mathrm{eV}$. Therefore, the color changes indicate a band gap that decreases with increasing strength of the bond. This variation is just opposite to that experienced in covalent elements crystallizing in the diamond structure. In general, stronger bonding (shorter bond lengths) increases the gap between the mean energies of the occupied bonding orbitals and the empty antibonding orbitals. Therefore, it is difficult to understand the color changes in the silver salts unless the top of the valence band is composed of nonbonding core orbitals-the $4 d$ or hybridized ( $4 d-5 s$ ) orbitals at the $\mathrm{Ag}^{+}$ions-rather than the bonding $\mathrm{O}^{2-}: 2 p$ orbitals. Since hybridization raises the $4 d$ levels relative to the $5 s$ levels, it should decrease the energy gap between the top of the $4 d$-like bands and the bottom of the 5 s-like bands, as illustrated schematically in Fig. 3. Therefore, if the top of the valence band is primarily $4 d$-like and reduction of the $\mathrm{Ag}-\mathrm{O}$ bond length requires greater $5 s$ hybridization, the energy gap $E_{g}$ will decrease with decreasing $\mathrm{Ag}-\mathrm{O}$ bond length, as observed. Furthermore, a relatively small energy


Fig. 3. Schematic energy diagrams for $\mathrm{Ag}^{+}$oxides: (a) long $\mathrm{Ag}-\mathrm{O}$ bonds, (b) short $\mathrm{Ag}-\mathrm{O}$ bonds $\left(\mathrm{Ag}_{2} \mathrm{O}\right)$.
separation between $4 d$ core orbitals and $5 s$ orbitals is required for appreciable deformation of the core via hybridization. Silver appears to be particularly susceptible to such a deformation of its core.

In $\mathrm{AgSbO}_{3}$, each oxygen forms two strongly covalent $\mathrm{Sb}-\mathrm{O}$ bonds. The $\mathrm{Sb}-\mathrm{O}_{1}-\mathrm{Sb}$ angle is only a little larger than $90^{\circ}$, and the remaining $p_{x}$ orbital perpendicular to the plane of that angle does not extend into the $\mathrm{M}^{+}$-ion tunnels. Therefore, ionic $\mathrm{Ag}-\mathrm{O}_{1}$ bond lengths are to be expected. The $\mathrm{Sb}-\mathrm{O}_{2}-\mathrm{Sb}$ angle, on the other hand, is somewhat larger than $120^{\circ}$, indicating strong hybridization of $s p^{3}$ orbitals at the $\mathrm{O}_{2}$ position. Moreover, the two remaining hybrid orbitals are directed into the tunnels where they can induce covalent $\mathrm{Ag}-\mathrm{O}$ bonding. Therefore, the short $\mathrm{Ag}_{2}-\mathrm{O}_{2}$ bonds are to be anticipated.

Several $\mathrm{MSbO}_{3}$ compounds having the cubic Im 3 structure have been prepared from $\mathrm{KSbO}_{3}$ by ion exchange. Table IV shows the lattice constants, obtained from both powder and singlecrystal X-ray data, for the various polymorphs having space group Im3. With the exception of $\mathrm{LiSbO}_{3}$, the lattice constants scale with the $\mathrm{M}^{+}$-ion radii. The highly ionic, large ions $\mathrm{K}^{+}, \mathrm{Tl}^{+}$ and $\mathrm{Rb}^{+}$can be expected to occupy the $\mathrm{O}_{1}-\mathrm{O}_{2}$ and $\mathrm{O}_{2}-\mathrm{O}_{2}$ sites, as does the $\mathrm{Na}^{+}$ion, whereas the small $\mathrm{Li}^{+}$ion may tend to occupy a position in or near an $\mathrm{O}_{2}$ face, as does the $\mathrm{Ag}^{+}$ion. The presence of ionic $\mathrm{Li}^{+}$ions in octahedral-site faces would expand the cubic lattice parameter relative to the value extrapolated from $\mathrm{RbSbO}_{3}, \mathrm{KSbO}_{3}$ and $\mathrm{NaSbO}_{3}$. That a similar expansion is not found in $\mathrm{AgSbO}_{3}$ is attributed to the core deformation resulting from $\mathrm{Ag}-\mathrm{O}$ covalent bonding, which induces $4 d-5 s$ hybridization at the $\mathrm{Ag}^{+}$ions.

## IV. Comparisons with $\boldsymbol{\beta}$-Alumina

Of the 26 octahedral tunnel sites per primitive unit cell, only 12 are occupied by $\mathrm{M}^{+}$ions. Therefore, excellent three-dimensional conductivity can be anticipated. Our data provide the following comparisons between the $\mathrm{MSbO}_{3}$ compounds and the so-called super ionic conductor $\beta$ alumina:

1. In both, the $\mathrm{M}^{+}$ions can be ion-exchanged in molten salts and the exchanges are reversible, except for $\mathrm{AgSbO}_{3}$ which can be only partially exchanged. In silver $\beta$-alumina (7), the shortest $\mathrm{Ag}-\mathrm{O}$ distance is $2.424 \AA$, which is large enough to be primarily ionic, whereas in $\mathrm{AgSbO}_{3}$ the shortest $\mathrm{Ag}-\mathrm{O}$ distance $2.260 \AA$ is small enough to be primarily covalent. Moreover, the reduced band gap introduced by this covalence enhances the probability of doping the crystal, thereby introducing electronic as well as ionic charge carriers.
2. Both $\mathrm{LiSbO}_{3}$ and $\mathrm{Li}_{2} \mathrm{O} \cdot 11 \mathrm{Al}_{2} \mathrm{O}_{3}$ have lattice parameters anomalously larger than predicted from extrapolation of the parameters for the other $\mathrm{M}^{+}$ions.
3. In both, $\mathrm{M}^{+}$ions only partially occupy the available M positions. Sodium $\beta$-alumina contains four $\mathrm{Na}_{1}-\mathrm{O}_{2}$ distances greater than $2.71 \AA$ (8), whereas $\mathrm{NaSbO}_{3}$ has six $\mathrm{Na}_{2}-\mathrm{O}_{2}$ distances at $2.65 \AA$. These distances are all larger than the sum of the ionic radii. Moreover, in $\mathrm{Na}_{2} \mathrm{O}$ $11 \mathrm{Al}_{2} \mathrm{O}_{3}$ the $\mathrm{Na}^{+}$ions must pass through a common octahedral-site edge, whereas in $\mathrm{NaSbO}_{3}$ they pass through octahedral-site faces. Therefore, we may anticipate comparable ionic mobilities in the two structures.
4. In $\beta$-alumina, the $\mathrm{M}^{+}$ions are constrained to two-dimensional motion, whereas in $\mathrm{MSbO}_{3}$ they may move in three dimensions, the $\langle 111\rangle$ tunnels intersecting at common octahedral sites at the origin. Thus the $\mathrm{Na}^{+}$-ion transport mechanism is similar to the $\mathrm{Ag}^{+}$-ion diffusion in $\mathrm{RbAg}_{4} \mathrm{I}_{5}$, where the $\mathrm{Ag}^{+}$ions partially occupy a threedimensional network of tetrahedra sharing common faces (9). Similar diffusion paths exist in other silver halides and chalcogenides (10-14).
5. Surprisingly, structure refinements of sodium
$\beta$-alumina indicate about $29 \%$ excess sodium (7). Similarly, our intensity data indicate an excess sodium concentration of $28.7 \%$ in nominal $\mathrm{NaSbO}_{3}$. Nevertheless, electrical neutrality is maintained in both compounds. The location and charge-neutrality mechanism of the excess sodium has not been identified in either compound.
6. Preliminary ac measurements indicate that the ionic conductivity of $\mathrm{NaSbO}_{3}$ compares favorably with that found for $\mathrm{Na}_{2} \mathrm{O} \cdot 11 \mathrm{Al}_{2} \mathrm{O}_{3}$.
7. It is difficult to prepare dense ceramic speciments of $\beta$-alumina that do not develop leaks. It is also difficult to prepare dense ceramics of metastable $\mathrm{NaSbO}_{3}$, since not pressing is confined to the temperature interval $T<500^{\circ} \mathrm{C}$. A more fundamental difficulty is that ceramic $\mathrm{NaSbO}_{3}$ is slowly attacked by molten sodium. Nevertheless, the transport data demonstrate that "skeleton" structures of the Im3 type (here the $\mathrm{SbO}_{3}$ matrix forms the skeleton) promise to be important for fast-ion transport.

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[^1]:    ${ }^{a}$ Were obtained from GE XRD single-crystal diffractometer, the rest were obtained from powder diffractometer.

